

In SI unit $k = \frac{\mu_0}{4\pi}$ and In CGS system $k = 1$

$\mu_0 \rightarrow$ absolute magnetic permeability of free space

$$\mu_0 \rightarrow 4\pi \times 10^{-7} \text{ Wb A}^{-1} \text{ m}^{-1}$$

Imp Formulae.

$$dB = \frac{\mu_0}{4\pi} \frac{I dl \sin\theta}{r^2}$$

* Magnetic field due to a st. wire carrying currents-

Acc. to Biot-Savart's law

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \vec{r}}{r^3}$$

$$dB = \frac{\mu_0}{4\pi} \frac{I dl \sin\theta}{r^2}$$

In ΔPOC ,

$$\theta + \phi = 90^\circ$$

$$\theta = 90^\circ - \phi$$

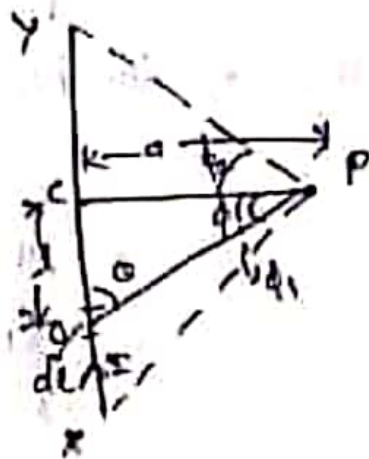
$$\sin\theta = \sin(90^\circ - \phi)$$

$$\sin\theta = \cos\phi$$

$$dB = \frac{\mu_0}{4\pi} \frac{I (a \sec^2 \phi d\phi) \cos\phi}{\left(\frac{a^2}{\cos^2 \phi}\right)}$$

$$dB = \frac{\mu_0}{4\pi} \frac{I}{a} \cos\phi d\phi$$

$$B = \int_{\phi_1}^{\phi_2} \frac{\mu_0}{4\pi} \frac{I}{a} \cos\phi d\phi$$



$$\Rightarrow \cos\phi = \frac{a}{r}$$

$$\therefore r = \frac{a}{\cos\phi}$$

$$\Rightarrow \tan\phi = \frac{l}{a}$$

$$l = a \tan\phi$$

$$dl = a \sec^2 \phi d\phi$$

$$B = \frac{\mu_0 I}{4\pi a} (\sin\phi_1 + \sin\phi_2)$$

⇒ Sp. Case ① when $\phi_1 = \phi_2 = 90^\circ$

$$B = \frac{\mu_0 I}{2\pi a}$$

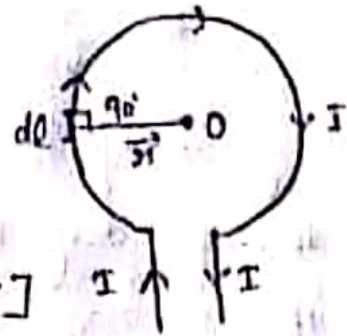
② when $\phi_1 = 90^\circ, \phi_2 = 0^\circ$

$$B = \frac{\mu_0 I}{4\pi a}$$

* Magnetic field at the centre of the circular coil carrying current :-

Acc. to Biot-Savart's law

$$dB = \frac{\mu_0 I dl \sin\theta}{4\pi r^2} \quad \text{--- (1)}$$



$$dB = \frac{\mu_0 I dl}{4\pi r^2} \quad [\theta = 90^\circ]$$

Integrating both sides

$$B = \int \frac{\mu_0 I dl}{4\pi r^2} = \frac{\mu_0 I}{4\pi r^2} \int dl$$

$$B = \frac{\mu_0}{4\pi} \times \frac{I}{r^2} \times 2\pi r = \frac{\mu_0}{4\pi} \times \frac{2\pi I}{r}$$

If the circular coil consist of 'n' turns, then

$$B = \frac{\mu_0}{4\pi} \times \frac{2\pi n I}{r}$$

* Magnetic field at a point on the axis of a circular coil carrying current :-

Acc. to Biot-Savart's law, the magnitude of magnetic field induction at point P, due to current element at c is given by