

$$\cot 90^\circ \Rightarrow 0 \quad \frac{\pi}{2} \times \frac{180}{\pi} = 90^\circ$$

$$(12) \cot(\tan^{-1} a + \cot^{-1} a)$$

$$\Rightarrow \cot\left(\frac{\pi}{2}\right) \quad \left[\because \tan^{-1} x + \cot^{-1} x = \frac{\pi}{2}\right]$$

$$\Rightarrow \underline{0} \text{ Ans}$$

$$(13) \tan \frac{1}{2} \left[ \sin^{-1} \frac{2x}{1+x^2} + \cos^{-1} \frac{1-y^2}{1+y^2} \right], \quad |x| < 1, y \geq 0 \text{ and } xy < 1$$

$$\Rightarrow \tan \frac{1}{2} [2 \tan^{-1} x + 2 \tan^{-1} y]$$

$$\Rightarrow \tan \frac{1}{2} \times 2 (\tan^{-1} x + \tan^{-1} y)$$

$$\Rightarrow \tan \left( \tan^{-1} \frac{x+y}{1+xy} \right)$$

$$\Rightarrow \boxed{\frac{x+y}{1+xy}} \text{ Ans}$$

$$(14) \text{ If } \sin \left( \sin^{-1} \frac{1}{5} + \cos^{-1} x \right) = 1, \text{ then find the value of } x.$$

~~$\frac{1}{5} = \sin y$~~

$$\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}$$

$$\boxed{x = \frac{1}{5}} \text{ Ans}$$

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$$(15) \tan^{-1} \left( \frac{x-1}{x-2} \right) + \tan^{-1} \left( \frac{x+1}{x+2} \right) = \frac{\pi}{4}$$

$$\Rightarrow \tan^{-1} \left( \frac{\frac{x-1}{x-2} + \frac{x+1}{x+2}}{1 - \left( \frac{x-1}{x-2} \right) \left( \frac{x+1}{x+2} \right)} \right) = \frac{\pi}{4}$$

$$\Rightarrow \tan^{-1} \frac{\frac{(x-1)(x+2) + (x+1)(x-2)}{(x-2)(x+2)}}{\frac{(x-2)(x+2) - (x-1)(x+1)}{(x-2)(x+2)}} = \frac{\pi}{4}$$

$$\Rightarrow \tan^{-1} \frac{x^2 + 2x - x - 2 + x^2 - 2x + x - 2}{x^2 + 2x - 2x - 4 - x^2 - x + x + 1} = \frac{\pi}{4}$$

$$\Rightarrow \frac{2x^2 - 4}{-3} = 1$$

$$\Rightarrow 2x^2 - 4 = -3$$

$$2x^2 = -3 + 4$$

$$2x^2 = 1$$

$$x^2 = \frac{1}{2}$$

$$x = \pm \frac{1}{\sqrt{2}} \quad \text{Ans}$$